

CHUKA



UNIVERSITY

UNIVERSITY EXAMINATIONS

EXAMINATION FOR THE AWARD OF DEGREE IN BACHELOR OF
SCIENCE IN ACTUARIAL SCIENCE

ACMT 202: FUNDAMENTAL OF ACTUARIAL MATHEMATICS II

STREAMS:

TIME: 2 HOURS

DAY/DATE: TUESDAY 18/4/2023

2.30 P.M. – 4.30 P.M.

Question One (30 Marks)

- a) Define a contingent payment model (2 marks)
- b) Consider a policy which consist of a payment of Kshs. 50,000 contingents upon retirement in 15 years. Suppose that the probability of a 45 years old to retire in 15 is 0.82 i.e. is ${}_{15}p_{45} = 0.82$. Find the actuarial present value of the contingent payment. Assume, a 6% interest compounded annually. (5 marks)
- c) A whole life insurance is used to (20) is payable at the moment of death. You are given (1) the time at death random variable is exponential with $\mu = 0.02$ (ii) $\delta = 0.14$.

Calculate (i) $\bar{A}_{20}$ (ii) ${}^2A_{20}$ and $\text{Var}(\bar{Z}_x)$ (8 marks)

- d) Define an n-year term life insurance. Deduce its present random variable, its actuarial present value and its variance. (8 marks)
- e) The age of death random variable is exponential with parameter 0.5. A life aged 35 buys 25year life insurance policy that pays I upon death. Assume an annual effect interest rate of 7%. Find the actuarial present value of this policy. (5 marks)

- f) . What is an endowment policy? Give two types of endowment policies. (2 marks)

Question Two (20 marks)

- a) . Define a term life insurance and state its,
- i). Present value random variable.
 - ii). The actuarial present value.
 - iii). Its second moments
 - iv). Its variance (10 marks)
- b) . Let the remaining lifetime at birth random variable X be uniform on $(0,100)$. Let ${}_{101}Z_{30}$ be a contingent payment random variable for a life aged $x=30$. Find
- i). ${}_{101}A_{30}$
 - ii). ${}_{101}^2A_{30}$
 - $\text{Var}({}_{101}IZ_{30})$ if $\delta = 0.05$ (10 marks)

Question 3 (20 marks)

- a) Explain what is recursion relations for life insurance. Give two types of recursion relations (4 marks)
- b) Show that $\bar{A}_{x:n}^1 = vq_x + vP_x A_{x+1:n-1}^1$
- c) Define an annually increasing whole life insurance
- a. -
- d) Give that $K(x)$ is uniform on $(0,3)$. Calculate (IA_x) if force of interest $\delta = 0.05$
- e) Show that $\bar{A}_{1x:n}^1 = \frac{1}{\delta} (A_{x:n-1}^1 + A_{x:n-1}^1)$

Question 4 (20 marks)

- a) Explain what is meant by contingent annuities and give three types of contingent annuities (8 marks)

b) For a disability insurance claim

- i). The claimant will receive payment at the rate of Kshs. 20,000 per year, payable continuously as long as she remains disabled.
- ii). The length of payment period in years will be a random variable with pdf $f(t) = te^{-t}$
- iii). Payment begin immediately.
- iv). $\delta = 0.05$. Calculate the actuarial present value of the disability payments at the time of disability (6 marks)

c) Explain a continuously n-year temporary life annuity. Find it's the present value random variable and its actuarial present value (6 marks)

Question 5 (20 marks)

A. What is continuous n-year certain and life annuity. State is present value random variable (4mks)

B. You are given the following probability mass function of $k(x)$

K	0	1	2
Pr (kx) = k	0.2	0.3	0.5

Find

$\ddot{a}_x$

(8mks)

$a_{\overline{n}|d}$

(4mks)

${}_2\ddot{a}_x$

(4mks)

=

$E\left(\frac{\ddot{Y}}{2}\right)$

i_f

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i

=

0

.

0

5

x

C. Define a temporary life annuity $\ddot{a}_{x:\overline{n}|}$ and deduce its present value variable

D. Deduce the actuarial present value of whole life discrete annuity immediate.

End.