

CHUKA



UNIVERSITY

**UNIVERSITY EXAMINATIONS**

**EXAMINATION FOR THE AWARD OF DEGREE OF  
MASTERS OF AGRICULTURAL ECONOMICS**

**AGEC 851: ECONOMETRICS METHODS**

**STREAMS: M (AGEC)**

**TIME: 3 HOURS**

**DAY/DATE: MONDAY 03/12/2018**

**2.30 PM – 5.30 PM**

**INSTRUCTIONS:**

**Answer Question One and any other Three**

**Question One**

(a) Given the following regression model  $y = \hat{\beta}_0 + \hat{\beta}_1 x_1 + \hat{\beta}_2 x_2 + \varepsilon$

Required:

(i) Derive the residue sum of squares (RSS) and the resulting first order normal equations. [6 marks]

(ii) Represent the normal equations derived in (i) above in matrix format. [4 marks]

(b) Explain two assumption of generalized linear regression model (GLS) [4 marks]

(c) Given the following vector of stochastic terms:

$$[\varepsilon_1 \varepsilon_2 \dots \varepsilon_n]$$

Prove that

(i)  $E(\varepsilon) = 0$  and that [10 marks]

(ii)  $E(\varepsilon' \varepsilon) = \sigma^2 I_n$

- (d) (i) Explain the meaning of an integrated series and four properties of an integrated series. [6 marks]
- (ii) Discuss three properties of a white noise process in time series. [10 marks]

**Question Two**

- (a) You are given the following econometric model

$$Y_{n \times 1} = X_{n \times k} \beta_{k \times 1} + \varepsilon_{n \times 1} \quad (\text{matrix representation})$$

Required:

- (i) Derive the OLS estimator  $\hat{\beta}$  [5 marks]
- (ii) Prove that  $E(\hat{\beta}) = \beta$  [5 marks]
- (iii) Prove the Gauss Markov Theorem (Minimum variance of  $\hat{\beta}$ ) [10 marks]

**Question Three**

- (a) Faced with a dummy dependent variable, explain the consequences of using OLS estimation method. [10 marks]
- (b) Given the following time series process  $y_t = C + \varepsilon_t + \theta \varepsilon_{t-1}$   
 Where C and  $\theta$  are constants and  $\varepsilon_t$  is a white noise process.
- (i) What type of data generation process does it represent? [2 marks]
- (ii) Find mean and variance of  $y_t$  [8 marks]

**Question Four**

- (a) Briefly explain the major difference between OLS (Ordinary Least Square) and MLE (Maximum Likelihood Estimation) methods. [6 marks]
- (b) State the four main dummy dependent variable models. [8 marks]

- (c) Discuss the six types of data generation processes in time series. [6 marks]

**Question Five**

- (a) State and explain advantages of panel data. [10 marks]

- (b) Explain the following terms as used in econometrics:

- |       |                         |           |
|-------|-------------------------|-----------|
| (i)   | Heteroscedasticity      | [2 marks] |
| (ii)  | Unit root               | [2 marks] |
| (iii) | Autocorrelation         | [2 marks] |
| (iv)  | Stationarity            | [2 marks] |
| (v)   | Disturbance /error term | [2 marks] |
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