UNIVERSITY EXAMINATIONS

## EXAMINATION FOR THE AWARD OF DEGREE OF MASTERS OF ARTS IN GEOGRAPHY

GEOG 833: ADVANCED QUANTITATIVE METHODS
STREAMS: MA (GEOG)
TIME: 3 HOURS
DAY/DATE: TUESDAY 14/04/2020
8.30 AM - 11.30 AM

## INSTRUCTIONS:

## Answer Question One and any other Three Questions

1. (a) Define statistical hypothesis testing.
(b) Differentiate between the following terminologies:
(i) Eigen vector and Eigen value
[2 marks]
(ii) Covariance and variance
(c) Solve the following system of linear equations using the Cramer's rule.
[5 marks]
(d) Explain any four assumptions of a two-way ANOVA.
[4 marks]
2. (a) A study was conducted to find out the type of relationship between human geography and quantitative methods in Geography scores for geography students. The results are displayed in the table below

| Student | Human geography score | Quantitative method in geography score |
| :--- | :--- | :--- |
| 1. | 84 | 69 |
| 2. | 74 | 64 |
| 3. | 48 | 56 |
| 4. | 54 | 72 |
| 5. | 72 | 85 |
| 6. | 71 | 68 |
| 7. | 96 | 87 |


| 8. | 75 | 71 |
| :--- | :--- | :--- |
| 9. | 69 | 91 |
| 10. | 100 | 31 |
| 11. | 23 | 65 |
| 12. | 58 | 89 |
| 13. | 94 | 71 |
| 14. | 76 | 54 |
| 15. | 52 | 66 |
| 16. | 61 | 78 |
| 17. | 77 | 97 |
| 18. | 98 | 84 |
| 19. | 83 | 71 |
| 20. | 77 |  |

(i) Use Pearson's Product Moment Correlation to compute correlation between the two sets of scores.
[7 marks]
(ii) Work out the coefficient of determination and explain its significance [2 marks]
(b) Suppose you computed $\mathrm{r}=-0.624$ with 14 data points, test significance of the correlation coefficient.
[6 marks]
3. In an experiment to determine the relationship between packed cell volume and red blood cell count of 10 dogs, the following results were obtained:

| Packed cell volume <br> $(\mathrm{mm}$ ) X | 45 | 42 | 56 | 48 | 42 | 35 | 58 | 40 | 39 | 50 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Red blood cell count <br> (millions) Y | 6.53 | 6.3 | 9.52 | 7.5 | 6.99 | 5.9 | 9.49 | 6.2 | 6.55 | 8.72 |

(a) Find the equation of regression line on Y on X [3 marks]
(b) Draw the scatter diagram and graph the line.
[3 marks]
(c) Use the line to estimate Y when $\mathrm{X}=37$
[3 marks]
(d) calculate the correlation coefficient
[3 marks]
(e) Test the significance of the correlation coefficient
[3 marks]
4. Consider the following data from an experiment of five samples with four variates each

| A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- |
| 10 | 12 | 9 | 11 | 10 |
| 4 | 10 | 4 | 9 | 6 |
| 6 | 13 | 4 | 10 | 8 |
| 4 | 7 | 5 | 11 | 4 |

Based pm the $5 \%$ level of significance, are there significant differences between the means of the five samples given the table below
[15 marks]
5. The following data gives the number of hired workers in a company in thousands

| Year | Jan | Feb | mar | April | may | June | July | Aug | Sept | Oct | Nov | Dec |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1939 | 156 | 156 | 158 | 198 | 205 | 237 | 260 | 317 | 380 | 255 | 210 | 165 |
| 1940 | 146 | 157 | 159 | 202 | 227 | 232 | 283 | 260 | 345 | 340 | 195 | 151 |
| 1941 | 134 | 143 | 154 | 170 | 203 | 275 | 368 | 413 | 430 | 361 | 294 | 231 |
| 1942 | 160 | 162 | 172 | 171 | 210 | 244 | 374 | 394 | 476 | 339 | 332 | 236 |
| 1943 | 153 | 161 | 167 | 185 | 209 | 269 | 356 | 404 | 474 | 350 | 309 | 243 |
| 1944 | 165 | 178 | 184 | 185 | 207 | 285 | 359 | 385 | 460 | 349 | 315 | 236 |
| 1945 | 174 | 179 | 179 | 188 | 211 | 263 | 364 | 417 | 501 | 336 | 341 | 224 |
| 1946 | 176 | 174 | 172 | 188 | 240 | 290 | 388 | 422 | 468 | 357 | 343 | 248 |
| 1947 | 188 | 190 | 201 | 200 | 236 | 313 | 418 | 432 | 453 | 387 | 339 | 249 |
| 1948 | 196 | 187 | 183 | 205 | 239 | 306 | 388 | 436 | 484 | 436 | 373 | 250 |

(a) Express the data as yearly time series and find the corresponding equation of the trend line.
(b) Graph the trend line by the method of least of squares
(c) Find the trend value for each of the years listed.
6. (a) Use matrices to solve the simultaneous equations:

$$
\begin{aligned}
& x--y+5 \\
& -2 x+2 z=y-10 \\
& 3 x+6 y+7 z=14
\end{aligned}
$$

Calculate the covariance matrix for this 3-dimensional set of data [8 marks]

| Item number | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- |
| $x$ | - | -1 | 4 |
| $y$ | 2 | 1 | 3 |
| $z$ | 1 | 3 | -1 |

