## CHUKA



## EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF

## ECON 313: ADVANCED MICROECONOMICS THEORY

STREAMS:
TIME: 2 HOURS
DAY/DATE: TUESDAY 02/02/2021
11.30 A.M - 1.30 P.M.

## INSTRUCTIONS

- Answer question One and any other Two questions


## QUESTION ONE

1) Prove the following claims mathematically.
i. Marginal Cost (MC) curve cuts the Average Cost (AC) curve from below and at its minimal point
[4 points]
ii. The oligopolistic joint output is higher than the monopolistic output but lower than competitive output.
2) Consider the following expenditure function

Where $P_{1}$ and $P_{2}$ are the prices of the two goods $X_{1}$ and $X_{2}$ respectively and $U$ is the consumer utility.
i) Compute the Hicksian demand functions
ii) Calculate the Marshallian demand functions
iii) Derive the indirect utility function
[5marks]
b. Explain any Five (5) properties of profit function
[5marks]
[5mark]

## QUESTION TWO

1. If a firm's cost function is. Where $\mathrm{w}_{1}$ and $\mathrm{w}_{2}$ are the prices of the two inputs $\mathrm{X}_{1}$ and $\mathrm{X}_{2}$ respectively
i. What is the associated production function? [8 marks]
ii. A true production function is said to be concave and homogeneous of degree one in input prices. Is the production function derived in (a) above legitimate? Show your working
[6 marks]
b. Explain six (6) properties of cost function
[6 marks]

## QUESTION THREE

a) Write short notes according to how you understand the following terms
[10 Marks]
i. Roy's identity
ii. Slusky's compensation
iii. Hotelling's Lemma
iv. Cournot model
v. Bertrand model
b) The convexity condition of indifference curve ensures a unique solution (interior solution) for the consumer. However, there exists some special cases where interior solution is not possible. Describe these cases.
[6 Marks]

## QUESTION FOUR

a) Consider a market with three oligopoly firms. Suppose that the market demand curve is given by, where. Supposed that the marginal cost for each firm is C. Suppose these firms choose quantities as follows; first firm 1 chooses $q^{1}$. Then firms 2 and 3 observe $q 1$ and then simultaneously choose $\mathrm{q}^{2}$ and $\mathrm{q}^{3}$ respectively. Calculate the equilibrium quantities, price and profits.
[10 marks]
b) With aid of a well labeled diagrams show how the exchange between two individuals can result in pareto efficient allocation

