

CHUKA



UNIVERSITY

UNIVERSITY EXAMINATIONS

EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF

PHYS 313: ELECTRICITY AND MAGNETISM II

STREAMS:

TIME: 2 HOURS

DAY/DATE: MONDAY 4/12/2017

2.30 P.M – 4.30 P.M

INSTRUCTIONS:

- **Answer question one and any other two questions**
 1. (a) State any three applications of Gauss's law. [3marks]
 - (b) Derive an expression for electric potential V of a point charge Q. [4marks]
 - (c) Calculate the potential at a point 0.05 m inside a charged sphere of radius 0.1 m and volume charge density $2.4 \times 10^{-7} \text{C/m}^3$. [5marks]
 - (d) Distinguish between a conductor and a dielectric . [2marks]
 - (e) Derive an expression for the work done in changing the orientation of a dipole in electric field E from 90° to θ° . [4marks]
 - (f) Derive Gauss's law in the form

$$\int_S E \cdot da = \frac{Q}{\epsilon_0}$$
 [5marks]
 - (g) Write down Maxwell's equations of electromagnetism in their general differential form in a vacuum. [4marks]
 - (h) Explain the reason as to why charges only reside on the surface of a conductor. [3marks]

2. (a) Show that potential due to the dipoles at a point P is given by $V_p = \frac{Qa \cos \varphi}{4\pi\epsilon_0 r^2}$ [7marks]

(b) From the equation for potential due to a dipole at point P, show that the electric field component in the Z-direction is given by

$$E_z = \frac{p}{4\pi\epsilon_0} \left(\frac{3 \cos^2 \theta - 1}{r^3} \right) \quad [10marks]$$

(c) Explain any three types of filters. [3marks]

3. (a) Laplace equation in Cartesian rectangular coordinates is

$$\frac{\sigma^2 v}{\sigma x^2} + \frac{\sigma^2 v}{\sigma y^2} + \frac{\sigma^2 v}{\sigma z^2} = 0$$

Assuming that the solution of this equation is a product of three functions which are separately functions x,y and z. Show the most general form of this solution. [9marks]

(b) Derive an expression for electric field E at a point P outside a sphere of radius R and uniform volume charge density p. [7marks]

(c) Calculate the electric field at a point 0.001m from the surface of a charged sphere of radius 0.05 m and volume charge density is given by.

$$\rho_b = -\nabla \cdot P \quad [6marks]$$

(c) Derive the equation of continuity. [8marks]

5. (a) Starting from sphere's law, derive Maxwell electromagnetic equation . [8marks]
- (b) For a series arrangement of R,L and C circuit and given that $R = 3 \times 10^5 \Omega$, $L = 10^{-3} \text{ H}$ and $C = 60 \text{ PF}$. Calculate:
- (i) The total current in each arm when a voltage of 20 V r.m.s at a frequency of 0.1 MHz is applied. [5marks]
- (ii) The phase of the total current drawn from the generator. [5marks]
- (c) Define polarization. [2marks]
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