

**THIRD YEAR FIRST SEMESTER EXAMINATION FOR THE AWARD OF
BACHELOR OF SCIENCE COMPUTER SCIENCE / BACHELOR OF SCIENCE
APPLIED COMPUTER SCIENCE**

COMP 303: THEORY OF COMPUTATION

**STREAMS: BSC COMPUTER SCIENCE / BSC APPLIED COMPUTER SCIENCE
TIME: 2 HOURS**

DAY/DATE: MONDAY 11/12/2017

2.30 P.M – 4.30 P.M

INSTRUCTIONS:

- Answer Question ONE and any other TWO questions.
- Diagrams should be used whenever they are relevant to support an answer.
- Sketch maps and diagrams may be used whenever they help to illustrate your answer
- Do not write anything on the question paper
- This is a closed book exam, No reference materials are allowed in the examination room
- There will be No use of mobile phones or any other unauthorized materials
- Write your answers legibly and use your time wisely

SECTION A

ANSWER ALL QUESTIONS IN THIS SECTION

QUESTION ONE [30 MARKS]

- Identify and explain any three areas that benefit from Context Free Grammars .
[6 Marks]
- Using appropriate diagrams, differentiate between Deterministic Finite Automaton and Non Deterministic Finite Automaton.
[6 Marks]
- Describe the features of a Turing Machine.
[3 marks]
- Giving an example for each differentiate between a set and a tuple [4 Marks]

- e) Present the Mathematical definition of Start and Final States of DFAs. Explain each definition. [6 Marks]
- f) Briefly explain how Mathematicians contributed to the definition of the Computing Algorithm. [5 Marks]

SECTION B

ANSWER ANY TWO QUESTIONS FROM THIS SECTION

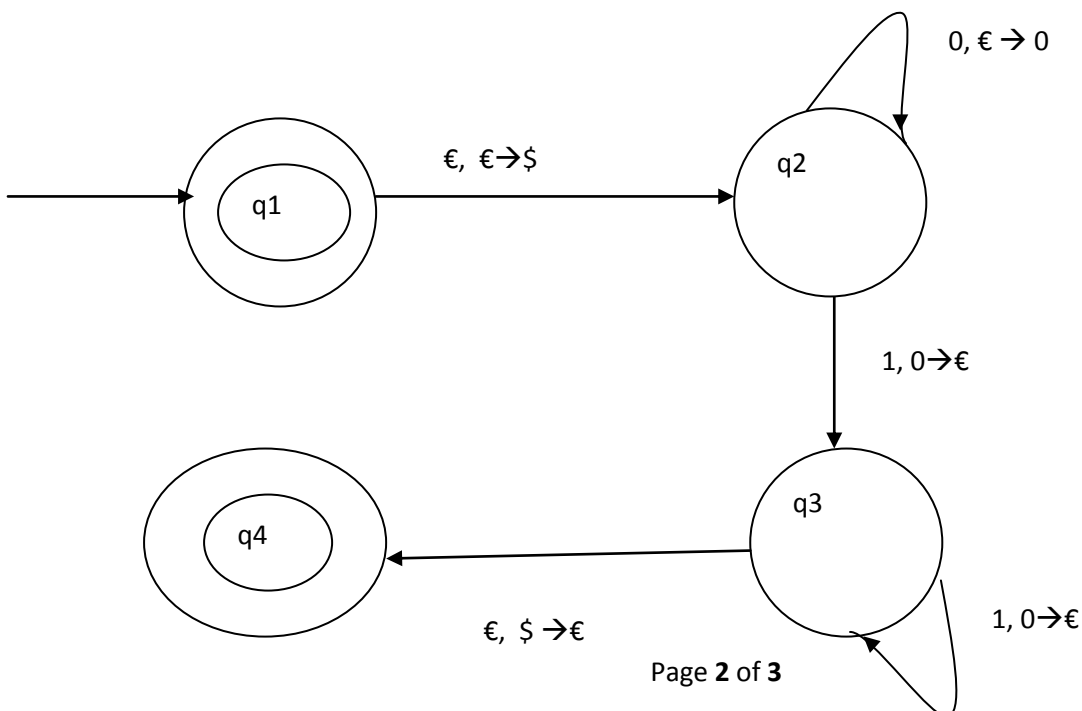
QUESTION TWO [20 MARKS]

- a) An Automatic door is one real life implementation of Finite Automaton computational model.
 - i. Explain the workings of an Automatic door. [2 Marks]
 - ii. Present the State diagram of such an Automatic door. [3 Marks]
 - iii. Formally define the State diagram of the Automatic door. [5 Marks]

- b) Explain how you would apply knowledge in the following to your computing profession:
 - i. Regular Expressions [3 Marks]
 - ii. Finite Automaton [2 Marks]
 - iii. Pumping Lemma [2 Marks]
 - iv. Kleene's theorem [3 Marks]

QUESTION THREE [20 MARKS]

- a) A pushdown Automaton PDA P is presented as follows:



Making reference to the Push Down Automaton above:

- a) Define the language accepted by PDA P [4 Marks]
- b) Discuss the computation of PDA P [10 Marks]
- c) Describe the relationship between PDA and other models of computation. [6 Marks]

QUESTION FOUR [20 MARKS]

- a) Explain the relationship between cryptography and the theory of complexity. [4 Marks]
- b) Compare and contrast Push Down Automata to the following computation models:
 - i. DFA [2 Marks]
 - ii. NFA [2 Marks]
 - iii. Turing Machines [2 Marks]
- c) Consider the context-free grammar $G = (V_1, \Sigma_1, R_1, S)$, where $V = \{A, B\}$, $\Sigma = \{0, 1\}$, A is the start variable, and R consists of the rules

$$A \rightarrow BAB | B | \epsilon$$

$$B \rightarrow 00 | \epsilon$$
 Convert this grammar to a Context-Free Grammar in Chomsky Normal Form whose language is the same as that of G . [10 Marks]

QUESTION FIVE [20 MARKS]

- a) Assume we have two regular languages $L(A) = \{\text{boy, girl}\}$ and $L(B) = \{\text{good, bad}\}$. Show the results of the regular operations below on the two languages:
 - i. Conjunction of Language $L(A)$ and Language $L(B)$ [2 Marks]
 - ii. Star of Language $L(B)$ [2 Marks]
- b) Describe the relationship between a computer virus and the theory of computability. [7 Marks]
- c) For each of the following languages, construct a DFA that accepts the language. In all cases, the alphabet is $\{0, 1\}$.
 - i. $\{w \mid \text{the length of } w \text{ is divisible by three}\}$ [3 Marks]
 - ii. $\{w \mid 110 \text{ is not a substring of } w\}$ [3 Marks]
 - iii. $\{w \mid w \text{ contains at least five } 1\text{s}\}$ [3 Marks]