CHUKA


UNIVERSITY EXAMINATIONS

## FOURTH YEAR EXAMINATION FOR THE AWARD OF DIPLOMA IN TOURISM AND DIPLOMA IN ANIMAL HEALTH

## MATH 0121: INTRODUCTORY MATHEMATICS

STREAMS: DTHM \& DIP. ANHE
TIME: 2 HOURS
DAY/DATE:
INSTRUCTIONS: ANSWER QUESTION ONE AND ANY OTHER TWO.SHOW YOUR WORKINGS CLEARLY

## QUESTION ONE

a) Expand $(2 x-3 y)^{4}[4$ marks]
b) Prove that $\sqrt{3}$ is not a rational number
c) Determine the domain and the range of the function $\left.\sqrt{\left(x^{2}\right.}-4\right)$
d) Simplify $\frac{6-3 i}{4-i}$ [4marks]
e) Find the value of K such that the sequence is an AP
[4marks]

$$
\mathrm{K}-1, \mathrm{~K}+3,3 \mathrm{~K}-1
$$

f) Distinguish between a simple and compound statement
g) Define the following properties of real numbers. State an example for each.

Distributive
Commutative
Associative
[6marks]

## QUESTION TWO

a) In a 6- question marking test how many different answer sheets are possible if no answer sheet can be used twice and there are
6 answer sheets available
7 answer sheets are available
10 answer sheets are available

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b) How many terms of the sequence $1,4,7,10 \ldots$ are needed to give a sum of 590 from the first term of the sequence
c) Find the quotient and the remainder when $\mathrm{x}^{3}-4 \mathrm{x}^{2}+\mathrm{x}+2$ is divided by $\left(\mathrm{x}^{2}-3\right)$
[5marks]
d) Prove analytically that $(A \cup B) U C=A \cup(B \cup C)$ [4marks]

## QUESTION THREE

a) A school committee of nine members is to be formed 8 parents and 6 teachers and the principal. In how many ways can the committee be formed in order to include
i) The principal
ii) The principal and 5 parents
[10marks]
b) Given $U=\{1,2,3,4,5,6,7,8,9,10\}$

$$
A=\{2,3,4\}
$$

$$
B=\{4,5,6\}
$$

Find i) $A^{c} \quad$ iv $(A \cap B)^{c}$
ii) $\left.B^{c} v\right) A^{c} \cap B^{c}$
iii) $\mathrm{A} \cap B \quad$ [6marks]
c) How many ways are there to select a first prize winner, second prize winner and a third prize winner from 50 different people who have entered a content

## QUESTION FOUR

a) The second term of a GP is 2 and the fourth term is 8 . Find the possible values of the common ratio and the corresponding first terms
b) Solve the following equation for $0^{\circ} \leq \theta \leq 360^{\circ}$ [6marks]

$$
2 \sin ^{2} \theta=\sin \theta
$$

c) Given that $\mathrm{f}(\mathrm{x})=2 \mathrm{x}-1$ and $\mathrm{g}(\mathrm{x})=\mathrm{x}+3$, find
i) $f \circ g(3)$
ii) $g \circ f(3)$
iii) $\operatorname{gog}(x)$
iv) $f o f(x)$

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## QUESTION FIVE

a) Construct a truth table for the following proposition to determine whether it is a fallacy, tautology or inderterminate
$(P \rightarrow Q) \leftrightarrow[\sim Q \rightarrow(\sim P \Lambda \sim Q)]$
[8marks]
b) A family of 4 brothers and 3 sisters is to be arranged for a photograph in one row. In how many ways can they be seated if
i) All the sisters seat together
ii) No two sisters seat together [4marks]
c) Given $z_{1}=3+4 i, z_{2}=-2 i+2$, find i) $z_{1}+z_{2}$

$$
\text { ii) } \mathrm{z}_{1}-\mathrm{z}_{2}
$$

iii) $Z_{1} Z_{2}$
iv) $z_{1} \mathrm{z}_{2}$ [8marks]

