## CHUKA



## UNIVERSITY

## UNIVERSITY EXAMINATIONS

## FIRST YEAR EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF SCIENCE AND BACHELOR OF EDUCATION

## MATH 141: INTRODUCTORY STATISTICS

STREAMS: B.ED \& BSC
TIME: 2 HOURS
DAY/DATE: TUESDAY 16/04/2019
8.30 A.M. - 10.30 A.M.

## INSTRUCTIONS:

- Attempt question one (compulsory) and any other TWO
- Do not write anything on the question paper
- Electronic calculators may be used


## QUESTION ONE (30 MARKS)

(a) With the help of relevant examples, state and explain the four scales of measurements in statistics.
(b) Distinguish between the following terms
(i) Discrete and continuous variables
(ii) Descriptive and inferential statistics
(iii) Population and sample
(c) An environmental study on a certain species of tree from mountain Kenya is summarized in the table given below.

| Marks | $30-39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ | $90-99$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 3 | 18 | 20 | 17 | 15 | 5 | 2 |

## Required:

| (i) | the mode | (2 marks) |
| :--- | :--- | :--- |
| (ii) | the median | $(2$ marks $)$ |
| (iii) | the standard deviation | $(3$ marks $)$ |
| (iv) | State two advantages of the median compared to the mean. | $(2$ marks $)$ |

(d) A box contains 3 red balls and 6 green balls. 3 balls are to be picked one after the other without replacement. Find the probability that;
(i) Three balls picked are of the same colour (3 marks)
(ii) At least 2 balls picked are green (3 marks)
(iii) Only one ball is red (2 marks)

## QUESTION TWO (20 MARKS)

(a) In a recent survey, 100 people were asked if they thought that the next Kenyan president should be a woman. The result of the survey is given below.

| Gender | Yes | No | Total |
| :--- | :---: | :---: | :--- |
| Male | 32 | 18 | 50 |
| Female | 8 | 42 | 50 |
| Total | 40 | 60 | 100 |

Find these probabilities:
(i) The respondent answered YES given that the respondent was a female.
(4 marks)
(ii) The respondent was a male, given that the respondent said NO. (4 marks)
(b) Consider the following data

| Class interval | Frequency |
| :--- | :---: |
| $90-99$ | 5 |
| $100-109$ | 8 |
| $110-119$ | 22 |
| $120-129$ | 27 |
| $130-139$ | 17 |
| $140-149$ | 9 |
| $150-159$ | 5 |
| $160-169$ | 5 |
| $170-179$ | 2 |

## Compute,

(i) The mean absolute deviation
(ii) Quartile deviation
(iii) The seventh decile
(iv) The $85^{\text {th }}$ percentile

## QUESTION THREE (20 MARKS)

(a) Discuss at least four roles of statistics in decision making process. Use relevant examples.
(b) A random sample of 64 students were selected and given IQ tests. The following are the IQ scores:

| 111 | 85 | 83 | 98 | 107 | 101 | 100 | 94 | 101 | 86 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 105 | 122 | 104 | 106 | 90 | 123 | 102 | 107 | 93 | 109 |
| 141 | 86 | 91 | 88 | 98 | 128 | 93 | 114 | 87 | 116 |
| 99 | 94 | 94 | 106 | 136 | 102 | 75 | 96 | 78 | 116 |
| 107 | 106 | 68 | 104 | 91 | 87 | 105 | 97 | 110 | 91 |
| 107 | 107 | 85 | 117 | 93 | 108 | 91 | 110 | 105 | 99 |
| 85 | 99 | 99 | 96 |  |  |  |  |  |  |

(i) Present the above data in a stem-and-leaf plot
(ii) From the plot, determine the most common IQ score range
(iii) Determine the range for the IQ scores
(c) A box contains 24 transistors, 4 of which are defective. If 4 are sold at random, find the following probabilities
(i) Exactly 2 are defective (2 marks)
(ii) All are defective
(2 marks)
(iii) None is defective
(2 marks)
(iv) At least 1 is defective
(2 marks)

## QUESTION FOUR (20 MARKS)

(a) The owner of a video store is interested in how many videos a typical customer watches during a year. She randomly selects the records of 90 customers and counts the number of videos rented during the previous year. The data are presented in the company table.

| 67 | 63 | 64 | 57 | 56 | 55 | 53 | 53 | 54 | 54 |
| :--- | :--- | :--- | ---: | :--- | :--- | :--- | :--- | :--- | :--- |
| 45 | 45 | 46 | 47 | 37 | 23 | 34 | 44 | 27 | 44 |
| 35 | 37 | 24 | 24 | 14 | 43 | 37 | 27 | 36 | 26 |
| 25 | 36 | 26 | 5 | 44 | 13 | 33 | 33 | 17 | 33 |
| 56 | 17 | 26 | 5 | 14 | 23 | 45 | 59 | 19 | 49 |
| 37 | 42 | 32 | 29 | 90 | 44 | 46 | 45 | 66 | 28 |
| 28 | 75 | 32 | 31 | 52 | 49 | 65 | 54 | 15 | 23 |
| 59 | 61 | 40 | 41 | 43 | 49 | 38 | 31 | 19 | 24 |
| 45 | 41 | 38 | 14 | 57 | 25 | 20 | 15 | 16 | 12 |

Construct a grouped frequency distribution using 5 to 9 as the lowest class. (5 marks) and hence compute:
(i) the $50^{\text {th }}$ percentile (2 marks)
(ii) the mode
(2 marks)
(iii) the mean and the standard variation
(b) A bag contains 4 black balls, 5 red balls and 4 green balls. If 4 balls are selected at random what is the probability that the 4 selected contain
(i) No red ball? (2 marks)
(ii) Exactly 1 black ball?
(2 marks)
(iii) Exactly 1 red ball and exactly 2 green balls

## QUESTION FIVE (20 MARKS)

(a) Explain the role of statistics in scientific research.
(b) A large Kenyan bank is planning on introducing a new word processing system to its secretarial staff. To learn about the amount of training that is needed to effectively implement the new system, the bank chose eight employees of roughly equal skill. These workers were trained for different amounts of time and were then individually put to work on a given project. The following data indicate the training times and the resulting times (both in hours) that it took each worker to complete the project.

| Training time (X) | Time to complete project (Y) |
| :--- | :--- |
| 22 | 18.4 |
| 18 | 19.2 |
| 30 | 14.5 |
| 16 | 19.0 |
| 25 | 16.6 |
| 20 | 17.7 |
| 10 | 24.2 |
| 14 | 21.0 |

(i) Compute and interpret the Pearson's correlation coefficient.
(ii) What is the estimated regression line?
(iii) Predict the amount of time it would take a worker who receives 28 hours of training to complete the project.

