

CHUKA



UNIVERSITY

UNIVERSITY EXAMINATIONS
**SECOND YEAR EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR
OF SCIENCE IN APPLIED COMPUTER SCIENCE**
ACSC 271: MATHEMATICS FOR COMPUTER SCIENTISTS
STREAMS: BSC APPLIED COMP SC
TIME: 2 HOURS
DAY/DATE: WEDNESDAY 4/12/2019
11.30 A.M – 1.30 P.M

INSTRUCTIONS
**Answer question one and any other two questions
Adhere to instructions on the answer booklet**
QUESTION ONE

(a) Obtain the domain of the following functions

(i) $f(x) =$ [2 marks]

(ii) $f(x) =$ [2 marks]

 (b) Given that $f(x) = 2 +$, obtain the inverse function of $f(x)$ and (3). [3 marks]

(c) Evaluate the limits of the following functions

(i) [4 marks]

(ii) [2 marks]

(d) Obtain the derivative of the following functions

(i) $y =$ [2 marks]

(ii) $f(x) =$ [2 marks]

(e) Evaluate the following integrals

(i) [2 marks]

(ii) [2 marks]

(f) Show that the differential equation

$$2xydx + (1 +) dy = 0$$
 is exact hence solve it . [2 marks]

(g) Find the angle between the vectors

$$=3i +4j +5k$$

$$= i +6j +2k$$

[2 marks]

(h) Using row reduction solve the simultaneous equations below by row reduction.

$$= 7$$

$$= 3$$

[2 marks]

(i) Determine whether the series

is convergent by the ratio test.

[2 marks]

QUESTION TWO

(a) Approximate the integral of

with $n = 5$, using Simpson's rule and obtain the actual error to 4 decimal points.

[8 marks]

(b) Using the root test show that the series

is convergent

[3 marks]

(c) Obtain the characteristic equation of the matrix

$$A =$$

Hence find λ by the Cayley Hamilton theorem.

[7 marks]

(d) Sketch the graph of the function

$$f(x) =$$

Obtain $f(2)$

[2 marks]

QUESTION THREE

(a) Find the volume of the parallelepiped spanned by the vectors.

$$i+3j+2k, 4i-5j+6k \text{ and } 3i+5k+2j.$$

[4 marks]

(b) Discuss the consistency of the following systems of equations by row reduction hence solve it if found consistent.

$$x +3y +z = 10$$

$$2x - y -2z = -6$$

$$4x -2y +5z = 15$$

[6 marks]

(c) Find the value of t for which the vectors

$$=2ti + 4j +2k$$

$$= i+3k -j$$

[3 marks]

(d) Evaluate the area of the triangle with the following vertices A (1,3,1) , B (4,5,6) and C (3,2,4) [5 marks]

(e) Solve the differential equation

$$, \text{ given that } y(0) = 10$$

[2 marks]

QUESTION FOUR

(a) Evaluate all the eigen values and eigen vectors of the matrix.

$$A =$$

[13 marks]

(b) Prove that the services

is absolutely convergent by the ratio test.

[7 marks]

QUESTION FIVE

(a) Find the domain and range of the function

$$f(x) =$$

[3 marks]

(b) Evaluate the limits of the following functions

[3 marks]

(ii)

[2 marks]

(iii)

[2 marks]

(c) Obtain the derivative of the function $f(x) =$

[2 marks]

(d) Evaluate the derivative of the functions $f(x) =$ from first principles.

[3 marks]

(e) Find the equation of tangent and normal to the curve

$$Y= 6-3t -4 - \text{ at the point } (-2,4)$$

[3 marks]

(f) Find the turning points of the curve.

$y =$

[2 marks]
