

CHUKA



UNIVERSITY

**UNIVERSITY EXAMINATIONS**

**FIRST YEAR EXAMINATION FOR THE AWARD OF DEGREE OF MASTER OF SCIENCE (PHYSICS)**

**PHYS 841: ELECTRODYNAMICS**

**STREAMS: M.Sc. (PHYSICS) Y1S1**

**TIME: 3 HOURS**

**DAY/DATE: TUESDAY 04/12/2018**

**8.30 A.M. – 11.30 A.M.**

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**INSTRUCTIONS:**

- Answer ANY FOUR questions.
- Useful constants:  $\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$ ,  $\epsilon_0 = 8.854 \times 10^{-12} \text{ F.m}^{-1}$ , electronic charge =  $1.6 \times 10^{-19} \text{ C}$

**Question one (15 marks)**

- (a) With an expression discuss the Coulomb's law and explain the factors that determines its magnitudes. (3 marks)
- (b) Three identical equal charges,  $q_1 = q_2 = q_3 = Q$  are placed at the apex of an equilateral triangle of side  $y$ . Calculate the resultant force on a single charge at the apex of the triangle. (9marks)
- (c) What's the force on a 0.1C charge moving at velocity  $v = (10j - 20k) \text{ ms}^{-1}$  in a magnetic field  $B = (3i + 4k) \times 10^{-4} \text{ Teslas}$ . (3marks)

**Question two (15 marks)**

- (a) Discuss Biot- Savart law using an expression and explain its parameters. (3marks)

(b) Using Biot- Savart law, show that the expression for magnetic flux due to a circular current loop of radius  $\mathbf{R}$  at a point  $\mathbf{P}$ , a distance  $\mathbf{x}$  from the centre of current loop is given by;

$$\mathbf{B} = \frac{\mu_0 I R^2}{2(R^2 + x^2)^{3/2}}$$

where  $\mathbf{B}$  is the magnetic flux,  $\mathbf{x}$  is the distance from the wire at which magnetic field is to be determined while  $\mu_0$  is the permeability of free space (10marks)

(c) In 2 (b), determine the magnetic field when  $\mathbf{x} \gg \mathbf{R}$  and when  $\mathbf{x} = \mathbf{0}$ (2marks)

**Question three (15 marks)**

(a) Write a differential equation that a Green function  $G'(x; x')$  for Poisson's equation must satisfy, for Dirichlet boundary conditions. Include a statement of the boundary conditions. (5marks)

(b) A problem has Dirichlet boundary conditions. Derived the general solution to the Poisson equation for electrostatic potential  $\phi(x)$  using a Green's function? (5marks)

(c) In an electrostatics problem with Neumann boundary conditions, what is the simplest allowable boundary condition on the Green's function  $G'(x; x')$ ? Hint: The result must be consistent with the differential equation that G satisfies. (5marks)

**Question four (15 marks)**

(a) At the upper surface of the Earth's atmosphere, the time average magnitude of the Poynting vector  $\langle \mathbf{S} \rangle = 1.35 \times 10^3 \text{ W/m}^2$  that is the solar constant.

(i) Assuming that the Sun's electromagnetic radiation is a plane sinusoidal wave, what are the magnitudes of the electric and magnetic fields? (5marks)

(ii) What is the total time-averaged power radiated by the Sun if the mean Sun-Earth distance is  $R = 1.5 \times 10^{11} \text{ m}$  (3marks)

(b) Compute the intensity of the standing electromagnetic wave given by;  
 $E_y(x, t) = 2E_0 \cos(kx) \cos(\omega t)$  and  $E_x(x, t) = 2E_0 \cos(kx) \cos(\omega t)$  (7marks)

**Question five (15 marks)**

(a) An electric dipole with  $q_1 = 20 \mu\text{C}$  at  $(-d, 0)$  and  $q_2 = -10 \mu\text{C}$  at  $(+d, 0)$  is in a two dimensional Cartesian coordinate. Calculate the resultant electric field strength at a point with coordinates  $(x, y)$ . Take  $d = 1 \text{ m}$  and  $x = y = 2 \text{ m}$ . (7marks)

(b) Discuss the four Maxwell's equation of classical electromagnetism with a source (8marks)