CHUKA


UNIVERSITY

# THIRD YEAR EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF SCIENCE, ART AND EDUCATION 

## MATH 343: APPLIED STATISTICS

STREAMS: BSC, BED, BA
TIME: 2 HOURS
DAY/DATE: TUESDAY 06/04/2021
8.30 A.M. - 10.30 A.M.

INSTRUCTION: Answer Question One and any other TWO Questions

## QUESTION ONE (30 MARKS)

(a) Explain the following terms as used in statistical hypothesis
(i) Null and alternative hypothesis
(ii) Simple and composite hypothesis
(iii) Level of significance
(b) Alfafa (kind of plants grown as fodder for animal) yields of 6 test plots are 1.5, 1.9, 1.2, 1.4, 2.3 and 1.3 tons respectively per hectare. Use a critical region of $\alpha=0.05$ to test the hypothesis $H_{0}: \mu=1.8$ vs $H_{1}: \mu \neq 1$.8. Assume that the yields have a normal distribution
(c) The following data represent the change (in ml ) in the amount of carbon monoxide transfer in smokers with chickenpox over a one week period:
$\begin{array}{lllllll}33 & 2 & 24 & 17 & 4 & 1 & -6\end{array}$

Is there evidence of significant improvement in lung function
(i) If the data are normally distributed with alpha=10?
[4 marks]
(ii) If the data are normally distributed with alpha unknown?

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(d) The efficacy of a treatment for hypertension is to studied using a small clinical trial. 38 hypertensive patients were randomly allocated to either group 0 (Placebo control) or group 1(treatment) and a tree month follow-up study was carried out. At the end of the study the difference in blood pressure was measured for patients in each group and recorded. The summary of the results is presented below.

| Group | Sample size | Mean | Variance |
| :--- | :---: | :---: | :---: |
| 0 | 21 | -0.208 | $4.101^{2}$ |
| 1 | 17 | 3.953 | $4.630^{2}$ |

Is there evidence of significant improvement in the treatment group? At 5\% significance level [6 marks]
(e) A departmental store A has for competitors; B,C,D \& E. Store A hires a consultant to determine if the percentage of shoppers who prefer each of the five stores is the same. A survey of 1100 randomly selected shoppers is conducted and the results about which one of the stores shoppers prefer are as shown below.

| Store | A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No. of shoppers | 262 | 234 | 204 | 190 | 210 |

Is there enough using a significant level of $5 \%$ to conclude that the proportions are really the same?
[6 marks]

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## QUESTION TWO (20 MARKS)

(a) The following data is a sample of 11 loan applicants in a certain bank in Kenya. The applied loan is either approved or declined (status) against five risk variables namely age of applicants $\left(X_{1}\right)$, applicants gender $\left(X_{2}\right)$, amount of loan applied $\left(X_{3}\right)$, applicant's salary $\left(X_{4}\right)$ and proposed repayment period $\left(X_{5}\right)$ as shown below.

|  | Unstandardized Coefficients |  | Standardized Coefficients |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | B | Std. Error | Beta | t | Sig. |
| (Constant) | .793 | .246 |  | 3.225 | .002 |
| $X_{1}$ | -.040 | .066 | -.043 | -.607 | .546 |
| $X_{2}$ | .186 | .074 | -.201 | -2.511 | .014 |
| $X_{3}$ | .200 | .074 | .203 | 2.691 | .009 |
| $X_{4}$ | .685 | .053 | .883 | 12.992 | .000 |
| $X_{5}$ | .345 | .049 | .526 | 17.523 | .000 |
| R Square=0.740: |  | Adjusted R Square=0.727; | F-Statistic=59.687(.000) |  |  |

## Required

Write a report on Multiple regression function and interpret the results [10 marks]
(b) A study investigating the association between size of cars and country found the following frequency counts

|  | USA | JAPAN | UK | FRANCE |
| :--- | :---: | :---: | :---: | :---: |
| ECONOMY | 21 | 24 | 33 | 55 |
| COMPACT | 27 | 35 | 37 | 40 |
| FULL SIZE | 36 | 11 | 12 | 4 |
| LUXURY | 15 | 3 | 7 | 8 |

Is there sufficient evidence of a significant relationship between size of car and country?
[10 marks]

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## QUESTION THREE (20 MARKS)

(a) Patel is the manager of a bakery in Chuka town. He believes that the smell of fresh baking will encourage customers to purchase goods form his bakery. To investigate the this belief, he recorded the daily sales for ten weeks when all bakery windows are open and the daily sales for another ten weeks when all the windows are closed as shown below.

| Windows | 190.8 | 215.5 | 207.0 | 204.5 | 202.0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Open | 185.7 | 204.1 | 187.8 | 208.8 | 215.6 |
| Windows | 205.4 | 177.6 | 199.4 | 192.2 | 193.5 |
| closed | 192.8 | 172.2 | 169.2 | 181.8 | 200.6 |

Assuming that these data may be deemed to be random samples from normal populations with same variance, investigate the bakers belief at 5\% significance level. [10 marks]
(b) The data below represents a sample of mathematics achievement test scores and calculate grades for 10 independently selected Chuka University students.

| Math test score (X) | 72 | 82 | 93 | 65 | 76 | 89 | 81 | 58 | 95 | 91 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Final calculate grade (Y) | 75 | 79 | 84 | 71 | 82 | 91 | 85 | 68 | 90 | 92 |

## Required:

Test whether the achievement test scores and calculated grades are independent at 5\% significance level.
[10 marks]

## QUESTION FOUR (20 MARKS)

(a) The table of unit of fertilizer used and the units of yield in a science laboratory experience is as shown below.

| Fertilizer | 23 | 27 | 28 | 29 | 30 | 31 | 33 | 35 | 36 | 39 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Yield | 18 | 22 | 23 | 24 | 25 | 26 | 28 | 29 | 30 | 32 |

## Required:

(i) Determine the Pearson correlation coefficient between fertilizer(X) and Yield (Y)

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(ii) Using the results in b (i), test for the significance of the correlation coefficients at 5\% significance level
(b) Two random samples taken from two normal populations are as follows

| sample I | 20 | 16 | 26 | 27 | 23 | 22 | 18 | 24 | 25 | 19 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sample II | 17 | 23 | 32 | 25 | 22 | 24 | 28 | 18 | 31 | 33 | 20 | 27 |

Estimate the variances of the populations and test whether the two populations have equal variance at 5\% level of significance.
[10 marks]

## QUESTION FIVE (20 MARKS)

The data in the accompanying table relate mean yields of soybean plant obtained in response to the indicated levels of ozone exposure over the growing season.

| X | Y |
| :---: | :---: |
| 10 | 5 |
| 14 | 3 |
| 7 | 5 |
| 12 | 2 |
| 5 | 7 |
| 6 | 8 |

## Required

i. Fit a simple linear regression model
ii. Compute the ANOVA
iii. Compute coefficient of determination and make comment

