## CHUKA UNIVERSITY

## THIRD YEAR EXAMINATION FOR THE AWARD OF BACHELOR OF SCIENCE IN ECONOMICS \& STATISTICS

## MATH 343: APPLIED STATISTICS

STREAM: BSc (ECON \& STAT)
TIME: 2 HOURS

## INSTRUCTION: Answer Question One and any other TWO Questions

## QUESTION ONE (30 MARKS)

(a) An experiment was conducted to test the efficacy of chloromycetin in checking typhoid. In a certain hospital chloromycetin was given to 285 out of the 392 patients suffering from typhoid as shown below.

|  | Typhoid | No Typhoid | Total |
| :--- | :--- | :--- | :--- |
| Chloromycetin | 35 | 250 | 285 |
| No Chloromycetin | 50 | 57 | 107 |
| Total | 85 | 307 | 392 |

## Required

With the help of $\chi^{2}$, test at $5 \%$, test the effectiveness of chloromycetin in checking typhoid.
[6Marks]
(b) A certain kind of plants grown as fodder for animal had yields of 6 test plots has $1.5,1.9$, $1.2,1.4,2.3$ and 1.3 tons respectively per hectare. Use a critical region of $\alpha=0.05$ to test the hypothesis $H_{0}: \mu=1.8$ vs $H_{1}: \mu \neq 1$.8. Assume that the yields have a normal distribution
(c) The following data represent the change (in ml ) in the amount of carbon monoxide transfer in smokers with chickenpox over a one week period:

| 33 | 2 | 24 | 17 | 4 | 1 | -6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Is there evidence of significant improvement in lung function
(i) If the data are normally distributed with alpha $=10$ ?
(ii) If the data are normally distributed with alpha unknown?
[4marks]
[4marks]
(d) The advisor of Statistics club of a large college believes that the group consists of $10 \%$ freshmen, $20 \%$ sophomores, $40 \%$ juniors and $30 \%$ seniors. The membership for the club this year consisted of 14 freshmen, 19sophomores, 51 juniors and 16 seniors. At $\alpha=10 \%$ test the advisors conjecture.
(e) A departmental store A has for competitors; B,C,D \& E. Store A hires a consultant to determine if the percentage of shoppers who prefer each of the five stores is the same. A survey of 1100 randomly selected shoppers is conducted and the results about which one of the stores shoppers prefer are as shown below.

| Store | A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No. of shoppers | 262 | 234 | 204 | 190 | 210 |

Is there enough using a significant level of $5 \%$ to conclude that the proportions are really the same?
[6marks]

## QUESTION TWO (20 MARKS)

(a) The following data is a sample of 15 patients in a certain Health facility in Kenya. The level of illness is classified in stages (Efficacy) against two concentration variables namely CA Breast concentration $\left(X_{1}\right)$, and Health control concentration $\left(X_{2}\right)$ as shown below.

| Model Summary |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Model | $R$ | $R$ Square | Adjusted R Square | Std. Error of the Estimate |
| 1 | .953 ${ }^{\text {a }}$ | . 909 | . 895 | . 375 |

a. Predictors: (Constant), HEALTH CONTROL, CA BREAST CONC

| ANOVA ${ }^{\text {a }}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model |  | Sum of Squares | $d f$ | Mean Square | $F$ | Sig. |
| 1 | Regression | 18.173 | 2 | 9.086 | 64.637 | . $000{ }^{\text {b }}$ |
|  | Residual | 1.827 | 13 | . 141 |  |  |
|  | Total | 20.000 | 15 |  |  |  |
| a. Dependent Variable: EFFICACY |  |  |  |  |  |  |
| b. Predictors: (Constant), HEALTH CONTROL, CA BREAST CONC |  |  |  |  |  |  |


| Coefficients ${ }^{\text {a }}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model |  | Unstandardized Coefficients |  | Standardized Coefficients | $t$ | Sig. |
|  |  | B | Std. Error | Beta |  |  |
| 1 | (Constant) | 1.018 | . 177 |  | 5.736 | . 000 |
|  | CA BREAST CONC | . 064 | . 132 | . 173 | . 483 | . 637 |
|  | HEALTH CONTROL | . 547 | . 251 | . 784 | 2.184 | . 048 |

[^0]
## Required

Write a report on Multiple regression function and interpret the results [10Marks]
(b) A study investigating the association between size of cars and country found the following frequency counts

|  | USA | JAPAN | UK | FRANCE |
| :--- | :---: | :---: | :---: | :---: |
| ECONOMY | 21 | 24 | 33 | 55 |
| COMPACT | 27 | 35 | 37 | 40 |
| FULL SIZE | 36 | 11 | 12 | 4 |
| LUXURY | 15 | 3 | 7 | 8 |

Is there sufficient evidence of a significant relationship between size of car and country?
[10marks]

## QUESTION THREE (20 MARKS)

(a) Patel is the manager of a bakery in Chuka town. He believes that the smell of fresh baking will encourage customers to purchase goods form his bakery. To investigate the this belief, he recorded the daily sales for ten weeks when all bakery windows are open and the daily sales for another ten weeks when all the windows are closed as shown below.

| Windows | 190.8 | 215.5 | 207.0 | 204.5 | 202.0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Open | 185.7 | 204.1 | 187.8 | 208.8 | 215.6 |
| Windows | 205.4 | 177.6 | 199.4 | 192.2 | 193.5 |
| closed | 192.8 | 172.2 | 169.2 | 181.8 | 200.6 |

Assuming that these data may be deemed to be random samples from normal populations with same variance, investigate the bakers belief at 5\% significance level. [10marks]
(b) The data below represents a sample of mathematics achievement test scores and calculate grades for 10 independently selected Chuka University students.

| X | 72 | 82 | 93 | 65 | 76 | 89 | 81 | 58 | 95 | 91 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 75 | 79 | 84 | 71 | 82 | 91 | 85 | 68 | 90 | 92 |

## Required:

Test whether the achievement test scores and calculated grades are independent at 5\% significance level.
[10marks]

## QUESTION FOUR (20 MARKS)

(a) The table of unit of fertilizer used and the units of yield in a science laboratory experience is as shown below.

| Fertilizer | 23 | 27 | 28 | 29 | 30 | 31 | 33 | 35 | 36 | 39 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Yield | 18 | 22 | 23 | 24 | 25 | 26 | 28 | 29 | 30 | 32 |

## Required:

(i) Determine the Pearson correlation coefficient between fertilizer(X) and Yield (Y)
[4marks]
(ii) Using the results in $b$ (i), test for the significance of the correlation coefficients at 5\% significance level
[6marks]
(b) Two random samples taken from two normal populations are as follows

| sample I | 20 | 16 | 26 | 27 | 23 | 22 | 18 | 24 | 25 | 19 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sample II | 17 | 23 | 32 | 25 | 22 | 24 | 28 | 18 | 31 | 33 | 20 | 27 |

Estimate the variances of the populations and test whether the two populations have equal variance at $5 \%$ level of significance.
[10marks]

## QUESTION FIVE (20 MARKS)

The data in the accompanying table relate mean yields of soybean plant obtained in response to the indicated levels of ozone exposure over the growing season.

| X | Y |
| :---: | :--- |
| 10 | 5 |
| 14 | 3 |
| 7 | 5 |
| 12 | 2 |
| 5 | 7 |
| 6 | 8 |

## Required

i. Fit a simple linear regression model
ii. Compute the ANOVA
iii. Compute coefficient of determination and make comment

## CHUKA UNIVERSITY

FIRST YEAR UNIVERSITY EXAMINATION FOR THE AWARD OF DOCTOR OF PHILOSOPHY IN BUSINESS ADMINISTRATION

## DBAM 901: STATISTICS FOR RESEARCHERS

STREAM: Ph.D (Business Administration)
TIME: 3 HOURS
INSTRUCTION: Answer ANY Three Questions

## QUESTION ONE [20 MARKS]

a) Distinguish the following terms as used in Statistics
i. Descriptive and inferential statistics
[2 marks]
ii. Type I and Type II errors
[2 marks]
iii. Quantitate and Qualitative Data
b) The following table shows the distribution of masses of 40 logs of wood in a particular Town

| Mass(Kg) | $20-29$ | $30-39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 6 | 5 | 7 | 10 | 5 | 4 | 3 |

## Required

(i). Mean
(iii). Median
(v). Coefficient of Variation
(ii). Mode
(iv). Standard Deviation
c) The following data shows the annual sales reported by the three firms over a period of four years

|  | Sales (Kshs Millions) |  |  |
| :--- | :--- | :--- | :--- |
|  | Bidco Africa Ltd | Uniliver Ltd | Pwani oil Ltd |
| 2009 | 250 | 150 | 250 |
| 2010 | 200 | 180 | 200 |
| 2011 | 150 | 200 | 150 |
| 2012 | 200 | 250 | 150 |

## Required

Present the above information in a multiple bar Chart
[4 marks]

## QUESTION TWO [20 MARKS]

a) Outline 5 steps in Hypothesis testing
b) The advisor of Statistics club of a large college believes that the group consists of $10 \%$ freshmen, $20 \%$ sophomores, $40 \%$ juniors and $30 \%$ seniors. The membership for the club this year consisted of 14 freshmen, 19 sophomores, 51 juniors and 16 seniors. At $\alpha=10 \%$ test the advisors conjecture.
[5marks]
c) A market segmentation survey was conducted to test the model of rowing machine and the type of customer purchasing it as shown below.

|  | Customer type |  |  |
| :---: | :---: | :---: | :---: |
|  | Practical | Impulsive | Total |
| - Basic | 22 | 25 | 47 |
| . Designer | 13 | 88 | 101 |
| 3 3 Complete | 54 | 19 | 73 |
| ¢ Total | 89 | 132 | 221 |

## Required

Use Chi-square $\left(\chi^{2}\right)$ test at $5 \%$ significance level to find out if the model of rowing machine purchased is associated with type of customer.
[10 marks]

## QUESTION THREE [20 MARKS]

a) Outline 4 importance of regression analysis in Statistics/Management science [4 marks]
b) The demand and prices (in Kshs. thousands) for a bag of a hybrid 100kg bag of wheat in different regions of the country is as shown below.

| Price(X) | 56 | 60 | 62 | 65 | 70 | 80 | 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Demand (Y) | 138 | 148 | 150 | 156 | 153 | 160 | 173 |

## Required

(i) Fit a least square regression line $(Y=c+m X)$
[8 marks]
(ii) Suppose that you found a bag in one of the shops of the same kind of wheat costing Kshs 58,000, what would you approximate its demand in that area to be? [2 marks] (iii)Compute Pearson product moment correlation coefficient and make comment

## QUESTION FOUR [20 MARKS]

(a) A businessman who is almost bankrupt is trying to sell his business. He claims that the mean daily returns from the business is at least USD 4500.A prospective buyer conducts his own investigation and finds that during the next 20 days the mean return is USD 4300 with standard deviation of USD 400. Is there enough evidence to reject the businessman claim at 5\% significance level
[10 marks]
(b) Two random samples taken from two normal populations are as follows

| sample I | 20 | 16 | 26 | 27 | 23 | 22 | 18 | 24 | 25 | 19 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sample II | 17 | 23 | 32 | 25 | 22 | 24 | 28 | 18 | 31 | 33 | 20 | 27 |

Estimate the variances of the populations and test whether the two populations have equal variance at $5 \%$ level of significance.
[10marks]

## QUESTION FIVE [20 MARKS]

a) Briefly distinguish between Regression and correlation analysis
b) The following is a regression output on advertisement expenditure and sales of a certain firm in Kenya.

|  | Coefficient | Std <br> Error | $t$ - <br> statistic | p-value | Lower <br> $95 \%$ | Upper <br> $95 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Intercept | 65.71 | 27.73 | 2.37 | 0.033 | 4.67 | 126.74 |
| Advertising | 48.98 | 10.66 | 4.60 | 0.000 | 25.52 | 72.44 |
| Promotions | 59.65 | 23.63 | 2.53 | 0.024 | 7.66 | 111.65 |
| Competitors sales | -1.84 | 0.81 | -2.26 | 0.040 | -3.63 | -0.047 |
| $R^{2}=0.833$ <br> Adjusted $R^{2}=0.787$ <br> F-statistic $=18.290(0.000)$ |  |  |  |  |  |  |

## Required

Write a report on multiple regression function and interpret the results [10 marks]
c) The time taken to complete jobs of a particular type is known to be normally distributed with a mean of 6.4 hours and standard deviation of 1.2 hours. What is the probability that randomly selected job of this type takes;
i. Less than 6 hours
ii. Between 6 and 7 hours
iii. More than 7 hours


[^0]:    a. Dependent Variable: EFFICACY

