

UNIVERSITY

## UNIVERSITY EXAMINATIONS

FOURTH YEAR EXAMINATION FOR THE AWARD OF BACHELOR DEGREE IN MATHEMATICS AND BACHELOR OF EDUCATION SCIENCE

## MATH 444: DESIGNS AND ANALYSIS OF EXPERIMENT II

STREAMS: Bsc. MATHS
TIME: 2 HOURS
DAY/DATE : TUESDAY 28 /09/ 2021
11.30 AM - 1.30 PM

## INSTRUCTIONS

- Answer question one and any other two questions


## QUESTION ONE (30 MARKS)

a) Define the following terms as used in Designs of experiments.
(i) Balanced incomplete block designs. [2 Marks]
(ii) Response surface designs [2 Marks]
(iii) Lattice designs [2 Marks]
(iv) Simple lattice
[2 Marks]
b) (i) Outline the first six steps of analyzing a lattice design. [12 Marks]
c) Draw a general ANOVA of a partially Balanced incomplete block design. [4 Marks]
d) The table below shows a PBIBD with two associate classes.

| Block | Treatment |  |  |
| :--- | :--- | :--- | :--- |
| 1 | 1 | 2 | 4 |
| 2 | 1 | 2 | 3 |
| 3 | 3 | 4 | 6 |
| 4 | 3 | 4 | 5 |
| 5 | 1 | 5 | 6 |
| 6 | 2 | 5 | 6 |

(i) Draw an associate scheme [3 Marks]
(ii) Obtain two associate matrices

## QUESTION TWO [20 MARKS]

An Engineer uses a balanced incomplete block design to test performance of scars on 5 gasoline additives, due to time constraint.

## Car

| Additive | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | - | 17 | 14 | 13 | 12 |
| 2 | 14 | 14 | - | 13 | 10 |
| 3 | 12 | - | 13 | 12 | 9 |
| 4 | 13 | 11 | 11 | 12 | - |
| 5 | 11 | 12 | 10 | - | 8 |

Analyse the data at 5\% S.L and draw conclusions.

## QUESTION THREE (20 MARKS]

Perform the intrablock analysis for the following partially balanced incomplete block design at 5\% level of significance.

| Block |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Treatment | 1 | 2 | 3 | 4 | 5 | 6 |
| 1 | 14 | - | - | 10 | - | 16 |
| 2 | 10 | - | 12 | 15 | - | - |
| 3 | 20 | 24 | - | - | 19 | - |
| 4 | - | 16 | - | 11 | 10 | - |
| 5 | - | 13 | 17 | - | - | 12 |
| 6 | - | - | 9 | - | 10 | 8 |

## QUESTION FOUR [20 MARKS]

a) State and explain briefly two uses of response surface designs. [2 Marks]
b) The data below shows the factors used in an agricultural experiment and the yields there of .

| X (Nitrogen kg /ha) | 0 | 10 | 20 | 30 | 40 |
| :--- | :---: | :--- | :--- | :--- | :--- |
| Y (Yield kg/ha) | 775 | 1250 | 1375 | 1280 | 1200 |

(i) The coded values table
(ii) Obtain the Normal equations
(iii) The optimum level of nitrogen (coded)
(iv) Hence the optimum according to original units.

## QUESTION FIVE [20 MARKS]

(a) Analyse the following youden square design at 5\% level of significance. IS position significant?

| Blocks | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- |
| 1 | $\mathrm{~A}=2$ | $\mathrm{~B}=9$ | $\mathrm{C}=0$ | $\mathrm{D}=14$ |
| 2 | $\mathrm{~B}=6$ | $\mathrm{~A}=5$ | $\mathrm{E}=5$ | $\mathrm{C}=3$ |
| 3 | $\mathrm{C}=1$ | $\mathrm{D}=9$ | $\mathrm{~A}=0$ | $\mathrm{E}=7$ |
| 4 | $\mathrm{D}=8$ | $\mathrm{E}=8$ | $\mathrm{~B}=10$ | $\mathrm{~A}=4$ |
| 5 | $\mathrm{E}=7$ | $\mathrm{C}=6$ | $\mathrm{D}=11$ | $\mathrm{~B}=10$ |

