UNIVERSITY EXAMINATIONS

## EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF

## SOCI 302: INTRODUCTION TO SOCIAL STATISTICS

STREAMS: Y3S2
TIME: 2 HOURS
DAY/DATE: MONDAY 05/07/2021
8.30 A.M. - 10.30 A.M.

## INSTRUCTIONS:

- Answer question ONE and any other TWO questions.
- Use illustrations where appropriate.

1. (a) Briefly describe the following concepts:
(i) Correlational statistics
(2 marks)
(ii) Probability theory (2 marks)
(b) Distinguish between:
$\begin{array}{lll}\text { (i) } & \text { Descriptive statistics and inferential statistics } & (2 \text { marks }) \\ \text { (ii) } & \text { Discrete variables and continuous variables } & (2 \text { marks })\end{array}$
(c) In which scale can you measure the following:
(i) The religion of students in your class (1 mark)
(ii) Temperature measured on the Celsius scale (1 mark)
(d) Explain in detail the purpose of a measure of central tendency. (4 marks)
(e) Draw a negatively skewed distribution and indicate the approximate positions of the mean, the median and the mode on the curve.
(f) In two factories A and B located in the same industrial area, the average weekly wages and the standard deviations are as follows:

| Factory | Average | Standard Deviation | No. of workers |
| :--- | :--- | :--- | :--- |
| A | 34.5 | 5 | 476 |
| B | 28.5 | 4.5 | 524 |

(i) Which factory A or B pays out a larger amount as weekly wages? (2 marks)
(ii) Which factory A or B has greater variability in individual wages? (2 marks)
(g) Discuss four characteristics for a good or an ideal average. (4 marks)
(h) Describe the properties of measurement.
2. (a) According to National Population Census of Kenya for 1999, the Kenyan population in terms of age and sex is recorded as follows:

| Age | Male | Female | Total |
| :--- | :--- | :--- | :--- |
| $0-4$ | 1911216 | 1888827 | 3800043 |
| $5-9$ | 1744366 | 1725292 | 3468938 |
| $10-14$ | 1504044 | 1485648 | 2989692 |
| $15-19$ | 1177989 | 1704712 | 2378696 |
| $20-24$ | 989594 | 1013340 | 1902934 |
| $25-29$ | 782474 | 847287 | 1629761 |
| $30-34$ | 583173 | 575651 | 1159434 |
| $35-39$ | 464956 | 457942 | 918892 |
| $40-44$ | 367934 | 304244 | 233178 |
| $45-49$ | 235906 | 293405 | 574533 |
| $50-54$ | 179017 | 240657 | 476523 |
| $55-59$ | 150496 | 180055 | 360172 |
| $60-64$ | 113690 | 167901 | 318397 |
| $65-69$ | 82966 | 116980 | 230670 |
| $70-74$ | 66600 | 91212 | 174175 |
| $75+$ | 82210 | 60476 | 176280 |

Draw the histograms to show:
(a) Age-male distribution
(4 marks)
(b) Age-female distribution (4 marks)
(b) A study was done to determine the stress levels that students have while taking criminology exams. The stress level was found to be normally distributed with a mean level of 8.2 and a standard deviation of 1.34 . What is the probability that in the next criminology exam will have stress levels between 9 and 10 ?
(4 marks)
(c) If the accident rate at a certain factory is 7.0 and this is a Poisson process. Find the probability that fewer than 3 accidents occur in a year.
(4 marks)
(d) What is the probability that the sum of two dice is 4 given the first die is 2. (4 marks)
3.(a) Below is the distribution of persons according to different income groups. Calculate the arithmetic mean.
(4 marks)

| Income Kshs (100) | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of persons | 6 | 8 | 10 | 12 | 7 | 4 | 3 |

(b) Life of bulbs produced by two factories A and B are given below:

| Length of life (in hours) | Factory A (Number of bulbs) | Factory B (Number of bulbs) |
| :--- | :--- | :--- |
| $550-650$ | 10 | 8 |
| $650-750$ | 22 | 60 |
| $750-850$ | 52 | 24 |
| $850-950$ | 20 | 16 |
| $950-1050$ | 16 | 12 |
|  | 120 | 120 |

Bulbs from which factory have a more consistent length of life?
(8 marks)
(c) A company makes electric motors. The probability that an electric motor is defective is 0.01 . What is the probability that a sample contains?
(i) Exactly five defective motor.
(2 marks)
(ii) At most 10-defective motor.
(3 marks)
(iii) Six or more have burst tyres.
(3 marks)
4. (a) The grouped frequency table shows the length of service in years of employees who have been working for a company for at least ten years.

| Length of services (x) | $10-15$ | $15-20$ | $20-25$ | $25-30$ | $30-40$ | $40-50$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency (f) | 30 | 42 | 23 | 13 | 8 | 4 |

Calculate:
(i) Variance of the length of service of these employees.
(ii) Standard deviation of the length of service of these employees. (2 marks)
(b) The following is a frequency table showing the age distribution of members of a surveillance team

| Age | Frequency |
| :--- | :--- |
| $16-20$ | 6 |
| $21-25$ | 10 |
| $26-30$ | 8 |
| $31-35$ | 2 |
| $36-40$ | 1 |
| Total | 27 |

(i) Construct a frequency distribution table. (2 marks)
(ii) Calculate the relative frequencies and percentages for all classes. (2 marks)
(iii) Construct a histogram and frequency polygon.
5. (a) The following table gives the frequency distribution of 325 workers of a factory, according to their daily wages in a certain year.

| Income group (in Kshs) | Number of workers |
| :--- | :--- |
| Below 100 | 1 |
| $100-150$ | 20 |
| $150-200$ | 42 |
| $200-250$ | 55 |
| $250-300$ | 62 |
| $300-350$ | 45 |
| $350-400$ | 30 |
| $400-450$ | 25 |
| $450-500$ | 15 |
| $500-550$ | 18 |
| $550-600$ | 10 |
| 600 and above | 2 |
|  | 325 |

## Calculate median wage

(b) The data below shows the number of traffic crimes recorded at police stations, A and B in one week.

| No. of motor vehicles | Toll station A | Toll station B |
| :--- | :--- | :--- |
| $50-59$ | 15 | 43 |
| $60-69$ | 25 | 99 |
| $70-79$ | 40 | 54 |
| $80-89$ | 108 | 40 |
| $90-99$ | 92 | 14 |
| $100+$ | 20 | 0 |

(i) By means of Ogives compare the distribution of motor vehicles as recorded at the two stations.
(9 marks)
(ii) From the Ogives determine the frequency distribution below 60 and 90 traffic crimes for police stations, A and B, respectively.
(4 marks)
(iii) From the Ogives determine the class limits below 45\%.
(2 marks)

