c)Determine whether or not the vectors u = (1,1,2), w = (4,5,5) in R³ are linearly dependent

d) Reduce the following matrix to echelon form

$A = \begin{bmatrix} 1 & 2 & -3 & 0 \\ 2 & 4 & -2 & 2 \\ 3 & 6 & -4 & 3 \end{bmatrix}$

Find $u \times v$ and $u \times w$

 $C = \begin{bmatrix} \frac{1}{2} & -1 & -\frac{1}{3} \\ \frac{3}{4} & \frac{1}{2} & -1 \\ 1 & -4 & 1 \end{bmatrix}.$

b) Let u=2i-3j+4k, v=3i+j-2k, w=i+5j+3k

a) Compute the determinant

DAY/DATE: TUESDAY 6/07/2021

CHUKA

INSTRUCTIONS:

STREAMS: Y2 S2

- 2. Mobile phones are not allowed in the examination room.
- 1. Answer Question 1 and Any Other Two questions.

- 3. You are not allowed to write on this examination question paper.

SECTION A - ANSWER ALL QUESTIONS IN THIS SECTION **QUESTION ONE**

MATH 202 – FUNDAMENTALS OF LINEAR ALGEBRA



EXAMINATION FOR DEGREE OF

BACHELOR OF SCIENCE IN ACTUARIAL SCIENCE

MATH 202

UNIVERSITY

5.00 PM - 7.00 PM

TIME: 2 HOURS

(2 marks)

(6 marks)

(4 marks)



e) show that the below matrices are inverses

 $A = \begin{bmatrix} 1 & 0 & 2 \\ 2 & -1 & 3 \\ 4 & 1 & 8 \end{bmatrix} \text{ and } B = \begin{bmatrix} -11 & 2 & 2 \\ -4 & 0 & 1 \\ 6 & -1 & -1 \end{bmatrix}$

f)Define what is a vector subspace

g)

Let $A = \begin{bmatrix} 1 & -2 & 3 & 1 & 2 \\ 1 & 1 & 4 & -1 & 3 \\ 2 & 5 & 9 & -2 & 8 \end{bmatrix}$.

Use Gauss-Jordan to find the row canonical form of A

SECTION B - ANSWER ANY TWO QUESTIONS IN THIS SECTION

OUESTION TWO

a)Express $u=(1,-2,5)$ in \mathbb{R}^3 as a linear combination of the vectors.	
$u_1 = (1,1,1)$, $u_2 = (1,2,3)$, $u_3 = (2,-1,1)$	
b) Find all eigenvalues and corresponding eigenvectors of A	(6 marks)

b) Find all eigenvalues and corresponding eigenvectors of A

$$A = \begin{bmatrix} 2 & 2 \\ 1 & 3 \end{bmatrix}.$$

c)

Let $A = \begin{bmatrix} 2 & -2 \\ -2 & 5 \end{bmatrix}$, a real symmetric matrix.

Find an orthogonal matrix P such that $P^{-1}AP$ is diagonal. (9 marks)

QUESTION THREE

a) Evaluate the following system using Gaussian elimination. (3 marks)

> x + 2y - 4z = -42x + 5y - 9z = -103x - 2v + 3z = 11

(4marks)

(2 marks)

(9 marks)

b) Find solution using revised simplex method

(17 marks)

MAX Z= $3X_1 + 5X_2$ Subject to $X_1 \le 4$ $X_2 \le 6$ $3X_1 + 2X_2 \le 18$ And $X_1, X_2 \ge 0$

QUESTION FOUR

- a) Suppose u = (1,2,3,4) and v = (6,k,-8,2). Find k so that u and v are orthogonal. (3 marks)
- b) Suppose u=(1,-2,3) and v=(2,4,5). Find the distance, angle and projection (6 marks)
- c) Find the characteristic polynomial of the below matrix (6 marks)

$$A = \begin{bmatrix} 1 & 1 & 2 \\ 0 & 3 & 2 \\ 1 & 3 & 9 \end{bmatrix}.$$

d) Find the quadratic form q(x) that corresponds to the symmetric matrix (5 marks)

$$B = \begin{bmatrix} 4 & -5 & 7 \\ -5 & -6 & 8 \\ 7 & 8 & -9 \end{bmatrix}$$

QUESTION FIVE

a)Find the inverse (3 marks)

$$A = \begin{bmatrix} 5 & 3 \\ 4 & 2 \end{bmatrix}$$

b) Determine if A is an orthogonal matrix

$$A = egin{bmatrix} -1 & 0 \ 0 & 1 \end{bmatrix}$$

c)

Let
$$A = \begin{bmatrix} 1 & 2 \\ 4 & -3 \end{bmatrix}$$

 $f(x) = 2x^3 - 4x + 5$ and $g(x) = x^2 + 2x + 11$.

(5 marks)

Find		
Find i. ii.	A^2	
ii.	A^3	
iii.	f(A)	
iv.	g(A)	
		(12 marks)

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