

CHUKA



UNIVERSITY

UNIVERSITY EXAMINATIONS

**THIRD YEAR EXAMINATION FOR THE AWARD
OF BACHELOR OF SCIENCE IN LIBRARY SCIENCE**

MATH 100: GENERAL MATHEMATICS

STREAMS: BSC. LIBRARY

TIME: 2 HOURS

DAY/DATE: THURSDAY 01/04/2021

11.30 A.M. – 1.30 P.M.

INSTRUCTIONS*Instructions: Answer Question One and any other TWO Questions in Section B***SECTION A****QUESTION ONE (30 MARKS)**

- a) List all possible sets of real numbers in which all the following numbers belong
- i) $\sqrt{5}$ (1 mark)
 - ii) 16 (1 mark)
 - iii) -16 (1 mark)
 - iv) 0 (1 mark)
 - v) -3.333 (1 mark)
- b) Find the values of x in the following functions
- i) $2\log x = 4\log 3$ (2 marks)
 - ii) $\log_2(x - 1) = 5$ (2 marks)
 - iii) $\log_3(x - 2)^3 = \frac{1}{3}\log_3(4x + 7)$ (3 marks)
- c) Find the mean, mode, median, range, and standard deviation of the following data
30,50,30,70,20,50,30 (8 marks)
- d) The function $f(x) = ax^2 + x - 7$ has a remainder of 3 when divided by $(x-2)$. Find the value of 'a' (2 marks)
- e) Given $f(x) = 3x + 2$, $g(x) = x + 5$, find $f \circ g(x)$ (2 marks)
- f) Find $\frac{dy}{dx}$ for
- i) $y = 18x^6 + 9x^3 - \frac{1}{4x}$ (3 marks)

ii) $y = \sqrt[3]{x} + \frac{4}{x^3}$ (3 marks)

SECTION B

QUESTION TWO (20 MARKS)

Consider the following data representing the age of 100 people randomly selected in Chuka town.

Age	Frequency
0-9	5
10-19	8
20-29	7
30-39	12
40-49	28
50-59	20
60-69	10
70-79	10

Determine;

- i) Mean (2 marks)
- ii) Mode (3 marks)
- iii) Median (3 marks)
- iv) 75th percentile (3 marks)
- v) 7th decile (3 marks)
- vi) Semi-interquartile range (3 marks)
- vii) Standard deviation (3 marks)

QUESTION THREE (20 MARKS)

- a) Given $f(x) = 5x - 1$, $g(x) = x^2 + 4x$, $k(x) = \frac{1}{x-3}$. Find
- i) $(f \circ g)(-2)$ (4 marks)
 - ii) $(g \circ f)(-2)$ (4 marks)
 - iii) $(k \circ f)(5)$ (4 marks)
- b) Find the value of x in $ax^2 + bx + c = 0$ using completing square method (8 marks)

QUESTION FOUR (20 MARKS)

- a) The expression $x^3 + kx^2 - 2x - 4$ is fully divisible by $(x+1)$

- i) Find the value of k
ii) Use the long division method to confirm this result and hence solve the equation by using the value of k obtained in i) above (8 marks)
- b) Solve the following equations
- i) $2x^2 - 5x - 3 = 0$ (factorization method) (3 marks)
ii) $2x^2 + 5x = 3$ (completing square method) (3 marks)
iii) $9x^2 + 7x - 1 = 0$ (quadratic formula method) (3 marks)

QUESTION FIVE (20 MARKS)

- a) Simplify $\log \sqrt[3]{\frac{x^2y}{z^4}}$ (3 marks)
- b) Find the value of x in the following log functions
- i) $\log_2(x - 3) + \log_2(x - 1) = 3$ (3 marks)
ii) $\log_3(2x + 1) + \log_3(x + 8) = 3$ (3 marks)
- c) Find the derivatives of the following functions
- i) $p(x) = (x^2 + 2)(3x^2 - 5x)$ (3 marks)
ii) $Q(x) = \frac{5x^2}{4x+3}$ (3 marks)
iii) $h(t) = \left(\frac{2t+3}{6-t^2}\right)^3$ (5 marks)
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